



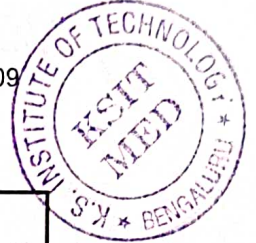
KAMMAVARI SANGHAM (R) - 1952  
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# K. S. INSTITUTE OF TECHNOLOGY

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#14, Raghuvanahalli, Kanakapura Main Road, Bengaluru - 560109



## BLUE BOOK

Name of the student : Bhavan Kashyap . K.

Class / Sem : VII 'A' Branch : Mechanical.

USN : 

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SUBJECT : Control engineering

SUBJECT CODE : 18ME71.

### MAXIMUM MARKS

Test	I	II	III	Average Marks Obtained
Date	27/10/22	28/11/22	22/11/22	Test
Marks Obtained	28/30	28/30	23/30	79/90 27/30
Signature of Student	<i>Bhavan Kashyap</i>	<i>Bhavan Kashyap</i>	<i>Bhavan Kashyap</i>	Assignment 10
Initials of Faculty	<i>Jhanky</i>	<i>Jhanky</i>	<i>Jhanky</i>	Total 37

NAME OF FACULTY : Dr. M. Umashankar

SIGNATURE OF FACULTY : *Jhanky*

SIGNATURE OF H.O.D. : *Jhanky*  
3/1/23

# K. S. INSTITUTE OF TECHNOLOGY

## First Internal Test

Q. No	Marks	CO	Q. No	Marks	CO	CO	Total
1(a)	06	Co1	3(a)		Co2	Co1 -	16
1(b)	<del>06</del> 06	Co1	3(b)		Co2		
1(c)	<del>04</del> 04	Co1	3(c)			Co2 -	12
OR			OR				
2(a)		Co1	4(a)	06	Co2		
2(b)		Co1	4(b)	06	Co2		
2(c)		Co1	4(c)			Grand Total	28/30

## Second Internal Test

Q. No	Marks	CO	Q. No	Marks	CO	CO	Total
1(a)	06	Co3	3(a)			Co3 -	18
1(b)	06	Co3	3(b)				
1(c)	06	Co3	3(c)			Co2 -	06
OR			OR				
2(a)			4(a)	06	Co2		
2(b)			4(b)	04	04		
2(c)			4(c)			Grand Total	28/30

## Third Internal Test

Q. No	Marks	CO	Q. No	Marks	CO	CO	Total
1(a)	06	Co5	3(a)			Co4 -	05
1(b)	06	Co5	3(b)				
1(c)	06	Co5	3(c)			Co5 -	18
OR			OR				
2(a)			4(a)	05	Co4		
2(b)			4(b)	00	Co4		
2(c)			4(c)			Grand Total	23/30

*J. Shanky*

Signature of the Faculty

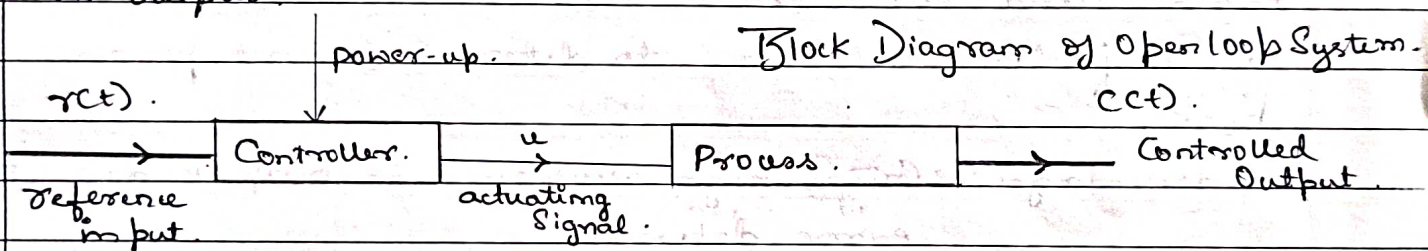
Part-A.

1a) Control system: Control means to regulate or direct or to command.

Hence control system is defined as arrangement of different physical components in such a way that / manner so is to regulate or to direct or to command itself to other systems.

→ Open loop Control system:

It is a type of control system whose output of a system is dependent on the input but input is not dependent on output.



Example - Toaster.

In a toaster reference input is applied as time and the heating of bread is considered as process and the controlled output is the Actual toast.

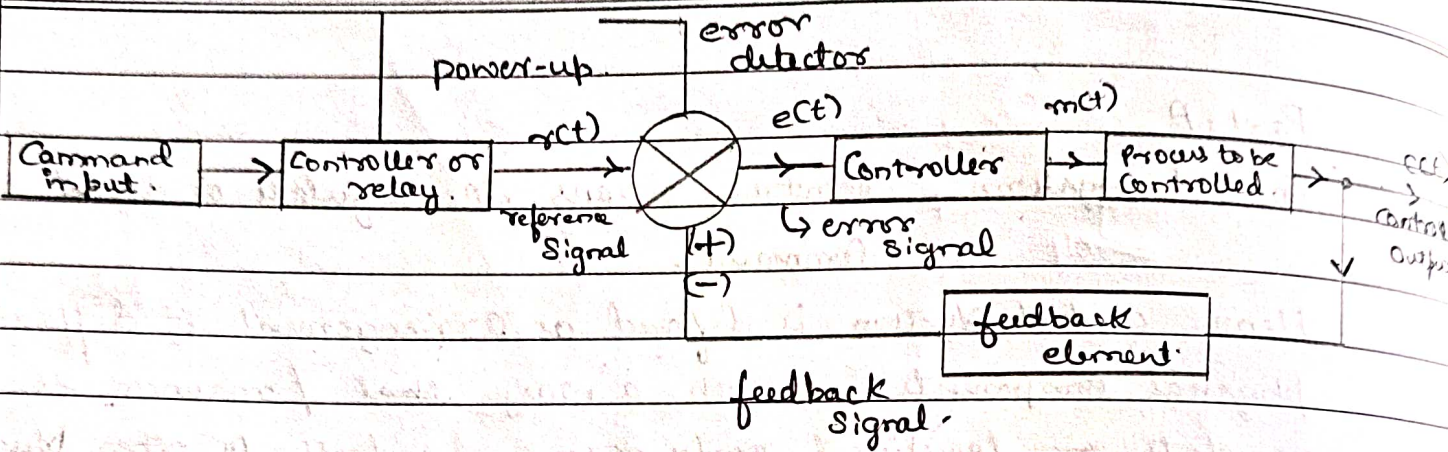
Advantages:

- Simple design
- Convenient to use.
- Easy maintenance.

Disadvantages:

- No accuracy in output.
- Variations in output due to environment changes.

→ Closed loop: It is a type of control system whose input is dependent on output and change in o/p.



### Block Diagram of Closed loop Control System

Ex: Human being.

In this case the output to be obtained is picking the book up. where input is feed to the controller in this case the brain and the transmitted to the hands where eye acts as a feedback element to determine exact position of the book.

Advantages: • Gives high accuracy in output due to error detector.

• Error detectors prevents the output to vary due to environment changes to obtain desired & appropriate output.

Disadvantages: • Complex design.  
• Requires skilled worker.  
• Comparitively difficult to maintain.

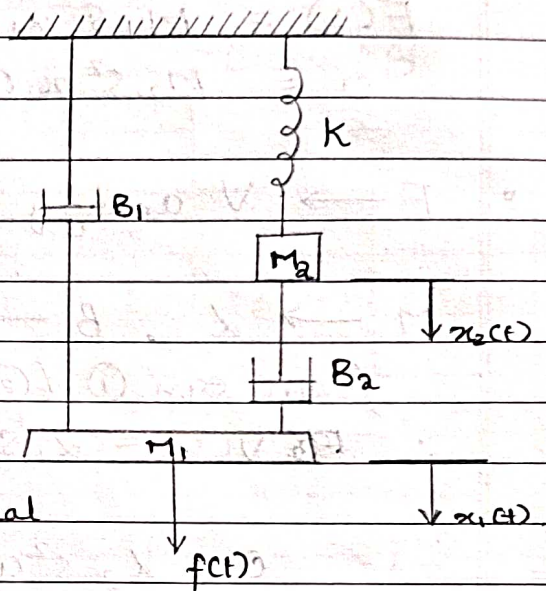
1b) To obtain:

• F - I } analogy.

• F - V

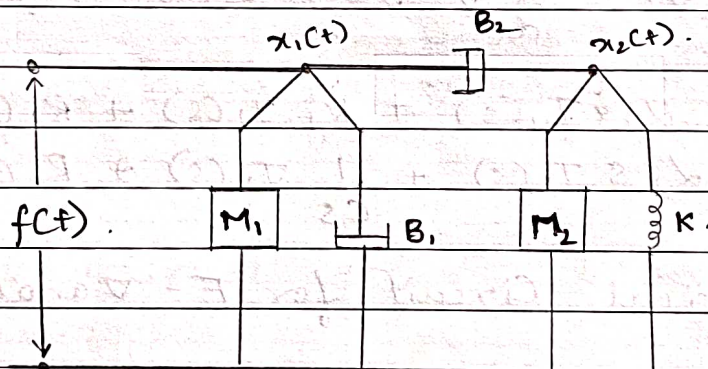
• and equilibrium equations.

Given:



for Given Mechanical Circuit.

The Equilibri Equivalent Mechanical Circuit is Given by.



Differential equation for Given Circuit (Equivalent).

$$f(t) = M_1 \frac{d^2 x_1(t)}{dt^2} + B_1 \frac{dx_1(t)}{dt} + B_2 \left( \frac{dx_1(t)}{dt} - \frac{dx_2(t)}{dt} \right)$$

$$0 = M_2 \frac{d^2 x_2(t)}{dt^2} + K (x_2(t)) + B_2 \left( \frac{dx_2(t)}{dt} - \frac{dx_1(t)}{dt} \right)$$

Applying Laplace transform.

$$F(s) = M_1 s^2 x_1(s) + B_1 s x_1(s) + B_2 (s x_1(s) - s x_2(s)) \rightarrow (1)$$

$$0 = M_2 s^2 x_2(s) + K x_1(s) + B_2 (s x_2(s) - s x_1(s)) \rightarrow (2)$$

•  $F \rightarrow V$  analogy (loop analysis).

$M \rightarrow \alpha$ ,  $B \rightarrow R$ ,  $K \rightarrow \frac{1}{C}$ ,  $F \rightarrow V$ ,  $x \rightarrow q$   
from eqn (1) & (2).

$$\therefore V(s) = \alpha_1 s^2 q_1(s) + R_1 s q_1(s) + R_2 (s q_1(s) - s q_2(s))$$

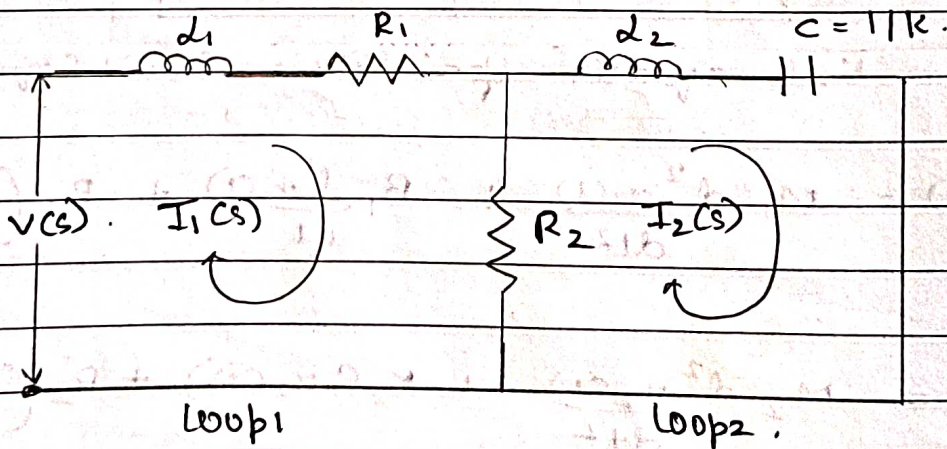
$$0 = \alpha_2 s^2 q_2(s) + \frac{1}{C} q_2(s) + R_2 (s q_2(s) - s q_1(s))$$

$$V(s) = \frac{dq_1}{dt} \text{ i.e. } I(s) = s q_1(s)$$

$$\Rightarrow V(s) = \alpha_1 s I_1(s) + R_1 I_1(s) + R_2 (I_1(s) - I_2(s)) \rightarrow (3)$$

$$0 = \alpha_2 s I_2(s) + \frac{1}{Cs} I_2(s) + R_2 (I_2(s) - I_1(s)) \rightarrow (4)$$

$\therefore$  Electrical Circuit for F-V analogy.



•  $F \rightarrow I$  analogy (Node analysis).

$M \rightarrow C$ ,  $B \rightarrow \frac{1}{R}$ ,  $K \rightarrow \frac{1}{L}$ ,  $F \rightarrow I$ ,  $x \rightarrow \phi$ .  
for eqn (1) & (2).

$$I(s) = C_1 s^2 \phi_1(s) + \frac{1}{R_1} s \phi_1(s) + \frac{1}{R_2} (s \phi_1(s) - s \phi_2(s))$$

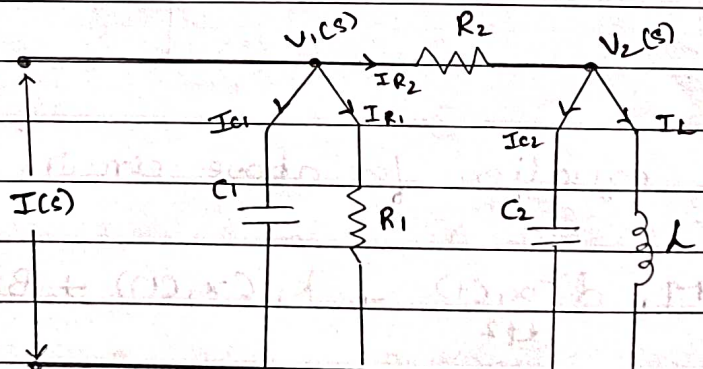
$$0 = C_2 s^2 \phi_2(s) + \frac{1}{L} \phi_2(s) + \frac{1}{R_2} (s \phi_2(s) - s \phi_1(s))$$

$$I(s) = \frac{d\phi}{dt}, \text{ i.e. } V(s) = s\phi(s)$$

$$I(s) = C_1 s V_1(s) + \frac{1}{R_1} V_1(s) + \frac{1}{R_2} (V_1(s) - V_2(s)) \quad \text{--- (5)}$$

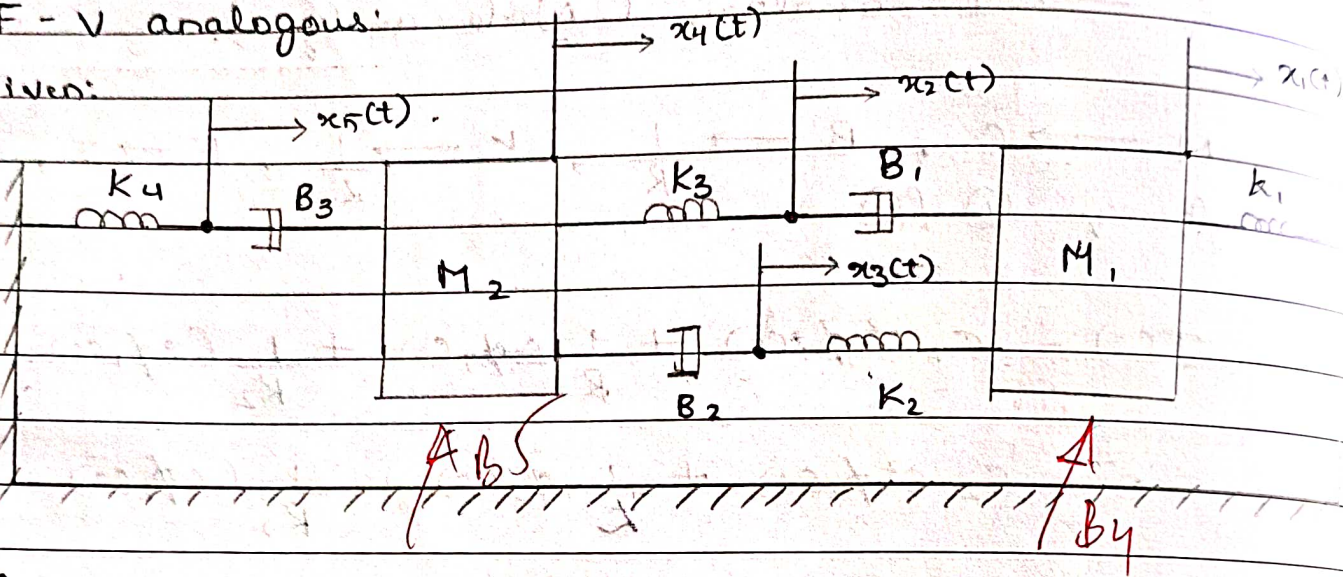
$$0 = C_2 s V_2(s) + \frac{1}{L} V_2(s) + \frac{1}{R_2} (V_2(s) - V_1(s)) \quad \text{--- (6)}$$

Electrical Circuit for  $F \rightarrow I$  analogy.

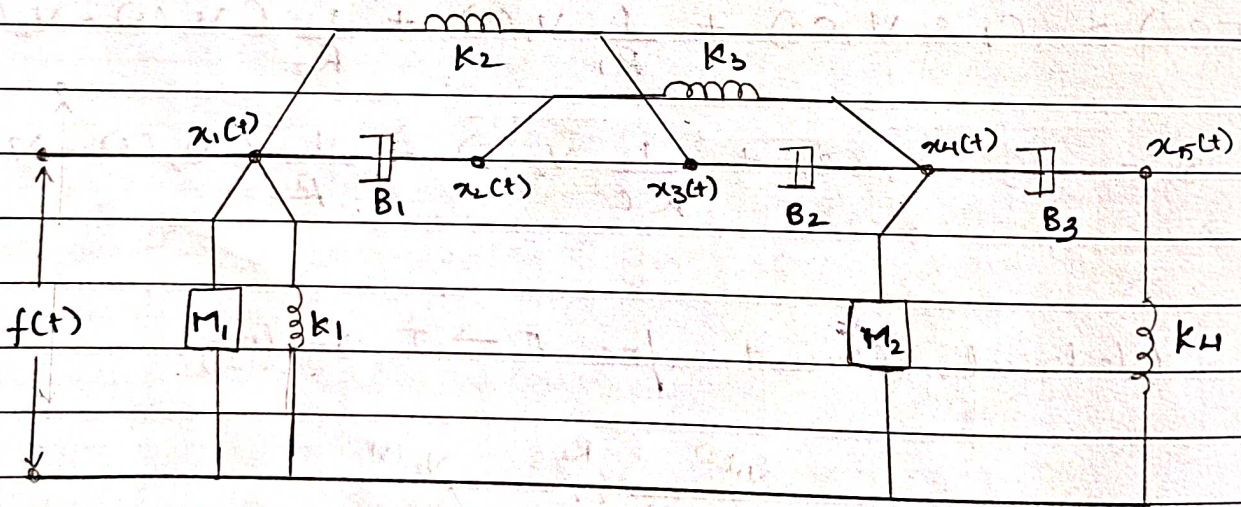


1c) F-V analogous:

Given:



for the Given Circuit  
Equivalent Mechanical Circuit is Given by.



Differential equation for above circuit.

$$f(t) = M_1 \frac{d^2 x_1(t)}{dt^2} + k_1 x_1(t) + B_1 \left( \frac{d x_1(t)}{dt} - \frac{d x_2(t)}{dt} \right) + k_2 (x_1(t) - x_2(t))$$

$$0 = B_1 \left( \frac{d x_2(t)}{dt} - \frac{d x_1(t)}{dt} \right) + k_3 (x_2(t) - x_4(t))$$



$$0 = K_2 (x_3(t) - x_1(t)) + B_2 \left( \frac{d x_3(t)}{dt} - \frac{d x_4(t)}{dt} \right)$$

$$0 = M_2 \frac{d^2 x_4(t)}{dt^2} + K_3 (x_4(t) - x_2(t)) + B_2 \left( \frac{d x_4(t)}{dt} - \frac{d x_3(t)}{dt} \right) + B_3 \left( \frac{d x_4(t)}{dt} - \frac{d x_5(t)}{dt} \right)$$

$$0 = K_4 (x_5(t)) + B_3 \left( \frac{d x_5(t)}{dt} - \frac{d x_4(t)}{dt} \right)$$

Applying Laplace transform.

$$F(s) = M_1 s^2 x_1(s) + K_1 x_1(s) + B_1 (s x_1(s) - s x_2(s)) + K_2 (x_2(s) - x_3(s)) \rightarrow (1)$$

$$0 = B_1 (s x_2(s) - s x_1(s)) + K_3 (x_2(s) - x_4(s)) \rightarrow (2)$$

$$0 = K_2 (x_3(s) - x_1(s)) + B_2 (s x_3(s) - s x_4(s)) \rightarrow (3)$$

$$0 = M_2 s^2 x_4(s) + K_3 (x_4(s) - x_2(s)) + B_2 (x_4(s) - x_3(s)) + B_3 (s x_4(s) - s x_5(s)) \rightarrow (4)$$

$$0 = K_4 (x_5(s)) + B_3 (s x_5(s) - s x_4(s)) \rightarrow (5)$$

for the above equations apply

$F \rightarrow V$  analogous (loop analysis)

$M \rightarrow L, B \rightarrow R, K \rightarrow \frac{1}{C}, F \rightarrow V, x \rightarrow q$

$$V(s) = L_1 s^2 q_1(s) + \frac{1}{C_1} q_1(s) + R_1 C s q_1(s) - s q_2(s) + \frac{1}{C_2} (q_1(s) - q_3(s))$$

$$0 = R_1 C s q_2(s) - s q_1(s) + \frac{1}{C_3} C q_2(s) - q_4(s)$$

$$0 = \frac{1}{C_2} C q_3(s) - q_1(s) + B_2 C s q_3(s) - s q_4(s)$$

$$0 = L_2 s^2 q_4(s) + B_2 C s q_4(s) - s q_3(s) + \frac{1}{C_3} (q_4(s) - q_2(s)) + B_3 (s q_4(s) - s q_5(s))$$

$$0 = \frac{1}{C_4} q_5(s) + B_3 C s q_5(s) - s q_4(s)$$

$$V(s) = \frac{dq}{dt}, \text{ i.e. } I(s) = s q(s)$$

~~Electrical Circuit for F-V analogy~~

$$V(s) = L_1 s C I_1(s) + \frac{1}{C_1 s} I_1(s) + R_1 C I_1(s) - I_2(s) + \frac{1}{C_2 s} C I_1(s) - I_3(s)$$

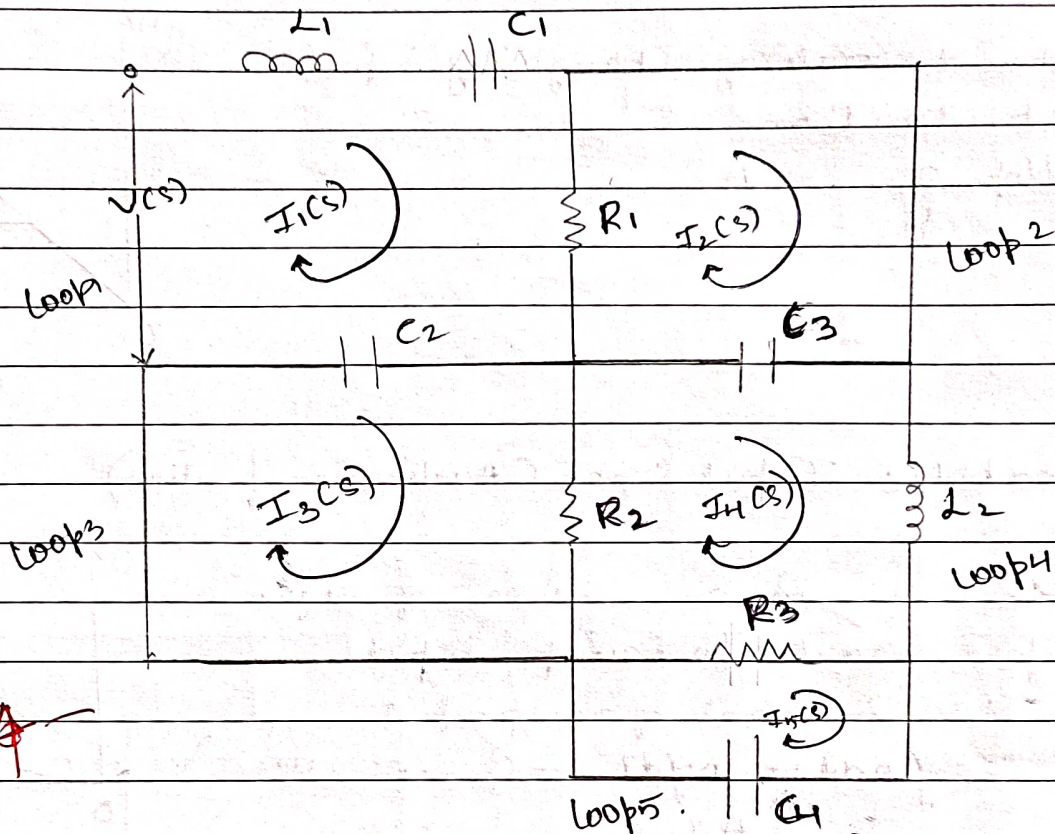
$$0 = R_1 C I_2(s) - I_1(s) + \frac{1}{C_3 s} C I_2(s) - I_4(s)$$

$$0 = \frac{1}{C_2 s} C I_3(s) - I_1(s) + B_2 (I_3(s) - I_4(s))$$

$$0 = L_2 s I_4(s) + B_2 C I_4(s) - I_3(s) + \frac{1}{C_3 s} C I_4(s) - I_5(s) + B_3 C I_4(s) - I_5(s)$$

$$0 = \frac{1}{C_4 s} C I_5(s) + B_3 C I_5(s) - I_4(s)$$

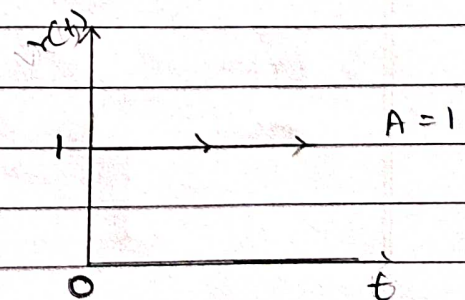
Electrical equivalent circuit for  $F \rightarrow V$



Part - B:

- 4a) Different input signals are
- Step input signal (position function) where sudden <sup>application</sup> increase in input is given

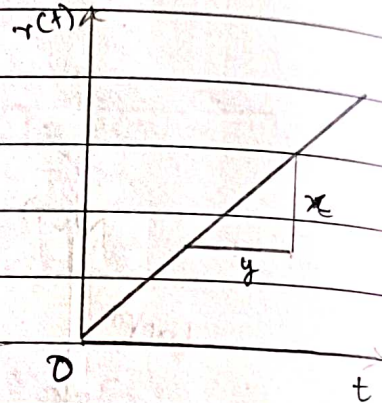
$$A \, dt = u(t) = 1 = A.$$



ii) Ramp Input Signal (Velocity function)

Constant rate of change of input w.r.t to time.

$$\text{Slope } \frac{x}{y} = A$$



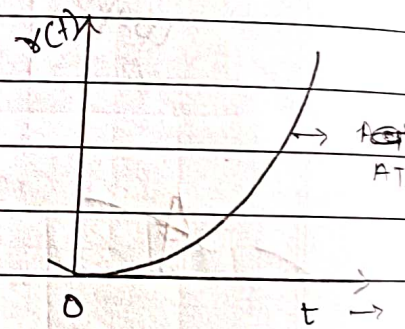
iii) Parabolic Input Signal (Acceleration function)

where there is an increase of <sup>one</sup> degree of input w.r.t to ramp input.

or it is integral of ramp input

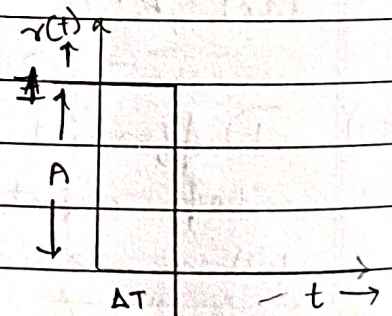
$$\int A dt = A \int dt$$

$$= A t$$



iv) Impulse input signal.

So Instantaneous increase in amplitude at a given interval of time.



06

4b) Steady state error.

Differential equation for 1<sup>st</sup> order time response is given

$$\frac{C(s)}{R(s)} = \frac{1}{Cs+T}$$

w.k.t the ramp input  $R(s) = \frac{1}{s^2}$

$$\therefore C(s) = \frac{1}{s^2(Cs+T)}$$

on further diff D.E.

$$C(s) = \frac{1}{s^2(Cs+T)} = \frac{A}{s^2} + \frac{B}{s} + \frac{C}{(s+T)} \rightarrow (1)$$

$$\therefore \frac{A \cancel{(Cs+T)}}{\cancel{s^2}} + \frac{B \cancel{(Cs^2)}}{\cancel{s}} + \frac{C \cancel{(Cs^2)}}{\cancel{(Cs+T)}} = 1$$

$$A(Cs+T) + B s(Cs+T) + Cs^2 = 1$$

$$\Rightarrow As + AT + Bs^2 + BTs + Cs^2 = 1$$

$$(A+BT)s + (B+C)s^2 + AT = 1$$

$$\therefore AT = 1 \Rightarrow A = \frac{1}{T} \rightarrow (2)$$

for  $(A+BT)s$

$$\Rightarrow \frac{1}{T} + BT = 0 \Rightarrow B = -\frac{1}{T^2} \rightarrow (3)$$

///<sup>ly</sup> for  $(B+C)s^2 = 0$

$$C = \frac{1}{T^2} \rightarrow (4)$$

Substituting (2), (3) & (4) in (1).

we get

$$V_0(s) = \frac{1/T^2}{s^2} + \frac{(-1/T^2)}{s} + \frac{1/T^2}{(s+T)}$$

Applying inverse transform

$$V_0(s) = \frac{1}{T^2} (t) + \left( -\frac{1}{T^2} \right) + \frac{1}{T^2} e^{-Tt} //$$

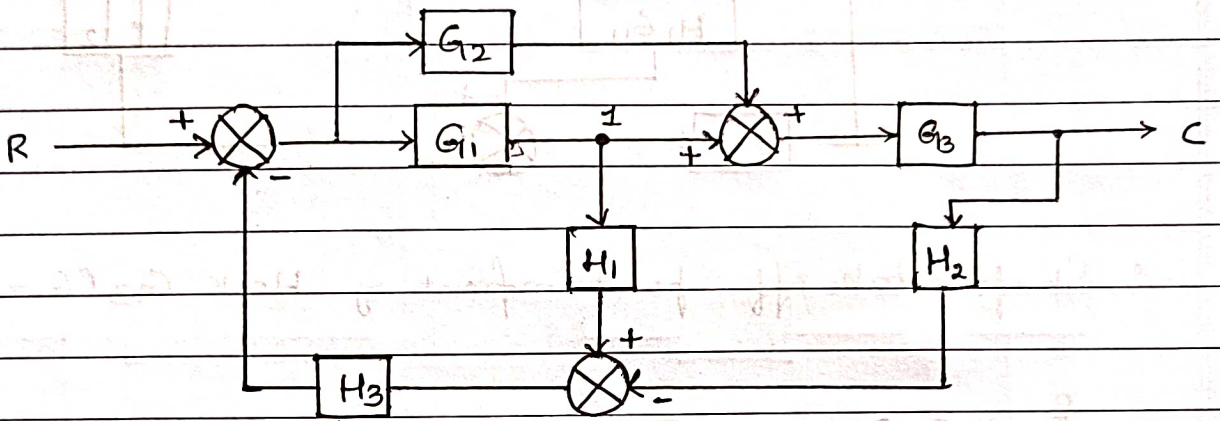
$\frac{28}{30}$

~~J. Khanna~~  
4/11/22

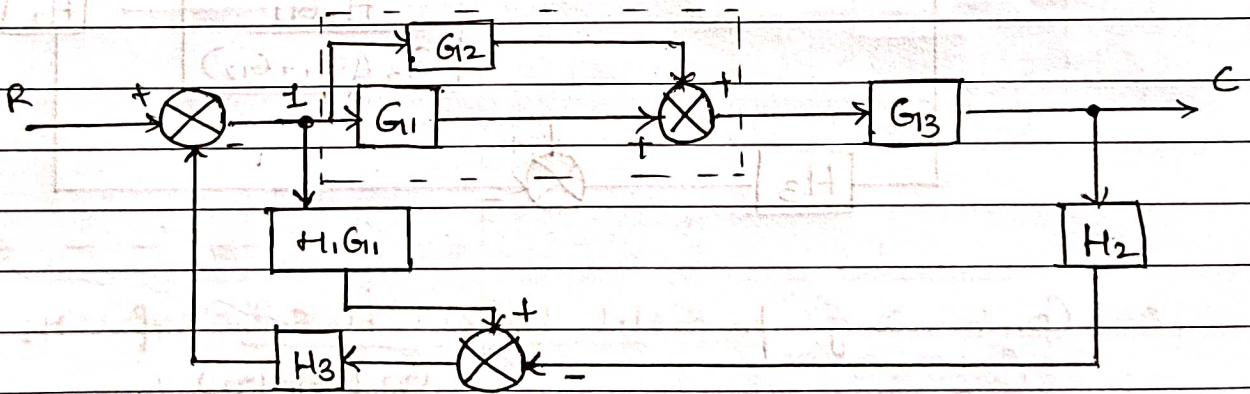
Intermale - II.

Part - A.

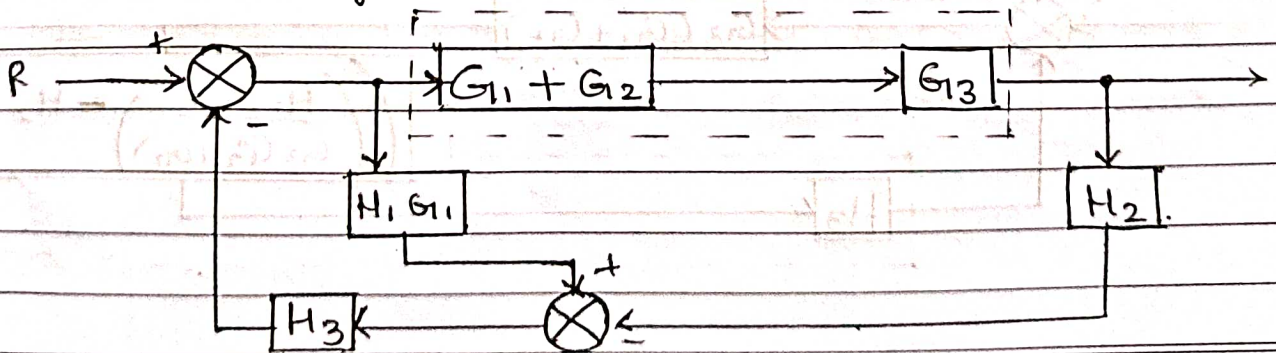
1a) Given.



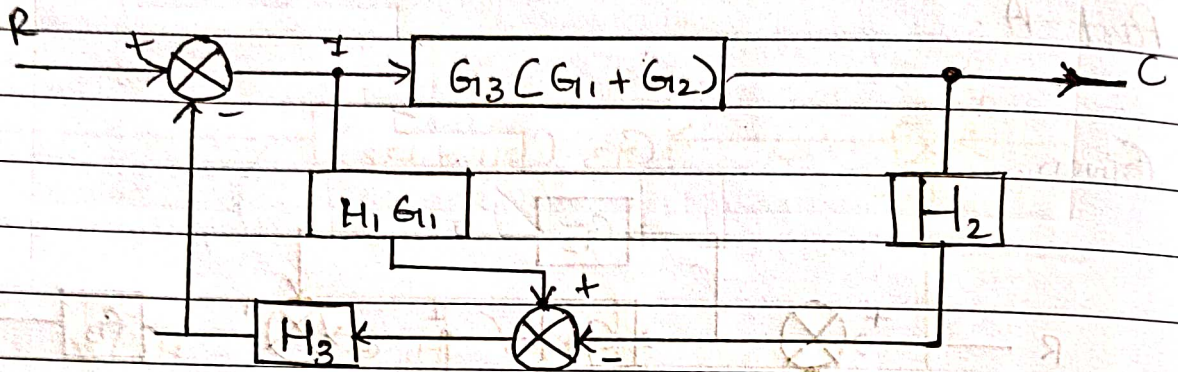
• Shifting take off point 1 Ahead of block  $G_1$ .



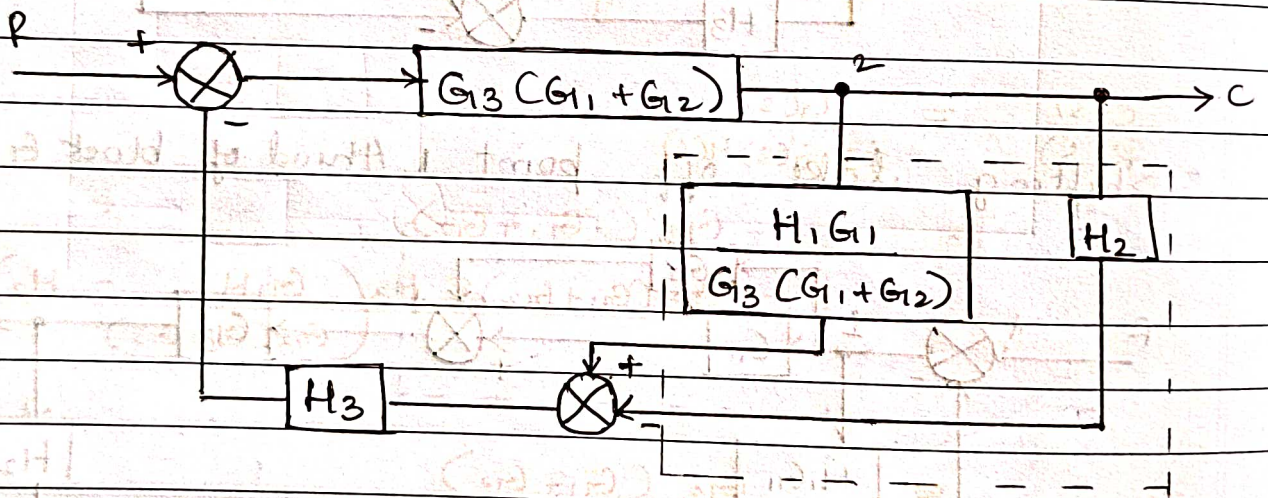
• Combining block  $G_1$  &  $G_2$ .



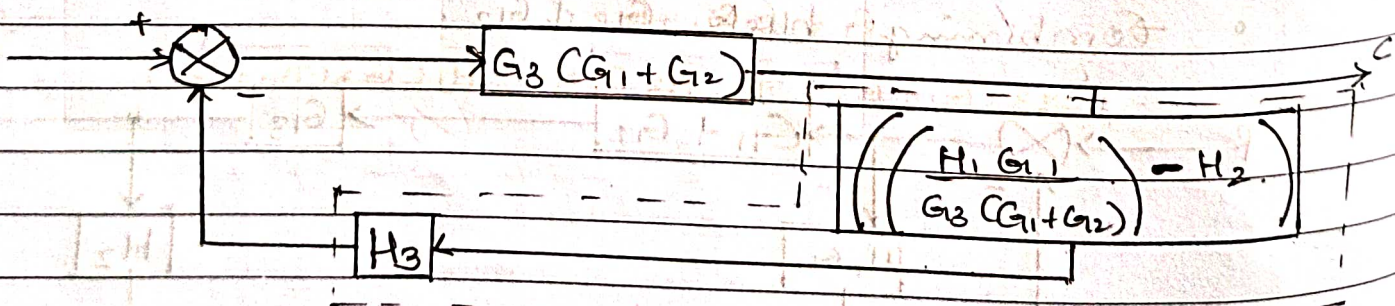
Combining block  $G_1 + G_2$  &  $B_3$



Shift take off point in front of block  $G_3(G_1 + G_2)$ .

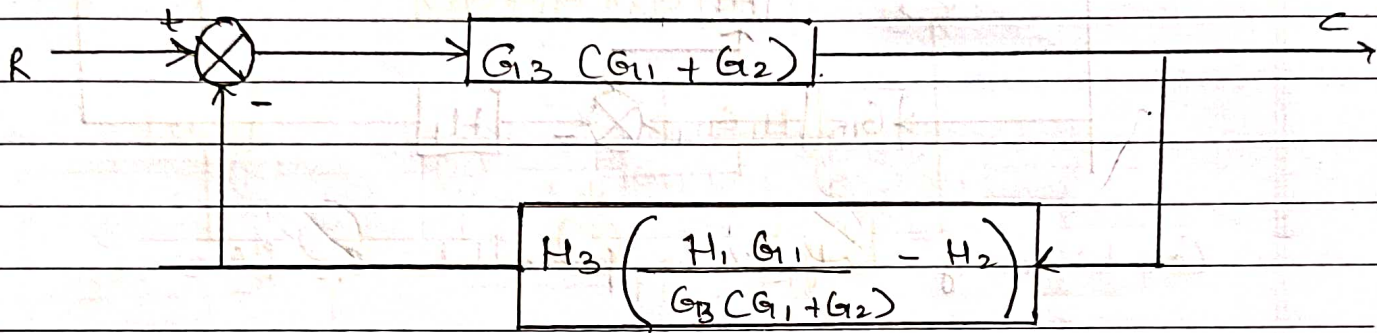


Combining parallel blocks  $H_1G_1$  &  $H_2$  over  $G_3(G_1 + G_2)$





- Combining two blocks in Series  $\frac{H_1 G_1}{G_1 G_2 + G_3} - H_2$  &  $H_3$



Now solving minor feedback loop. negal.

$$\frac{C(s)}{R(s)} = \frac{G(s)}{1 + G(s)H(s)}$$

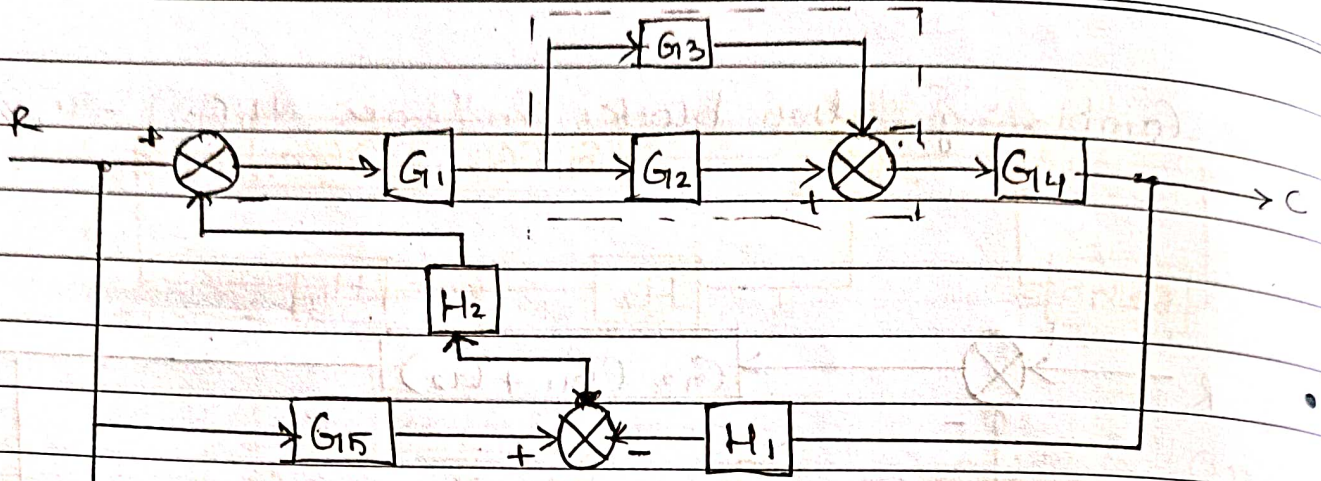
$$= \frac{G_3(G_1 + G_2)}{1 + G_3(G_1 + G_2) \cdot H_3 \left( \frac{G_1 H_1 - H_2}{G_3(G_1 + G_2)} \right)}$$

$$\Rightarrow \frac{G_3(G_1 + G_2)}{G_3(G_1 + G_2) + G_3(G_1 + G_2) \cdot H_3 \frac{G_1 H_1 - H_2}{G_3(G_1 + G_2)}}$$

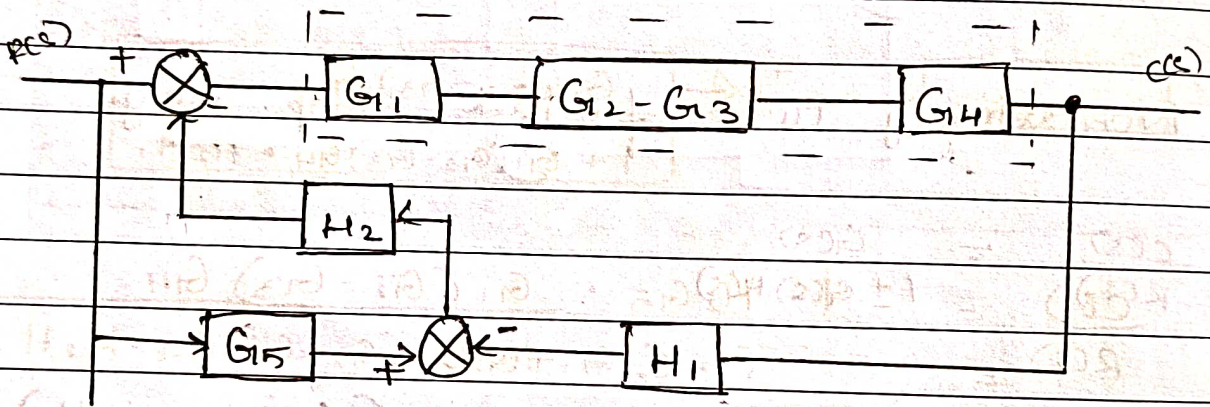
$$\Rightarrow \frac{G_3(G_1 + G_2)}{G_3(G_1 + G_2) + H_3(G_1 H_1 - H_2)} = \frac{C(s)}{R(s)}$$

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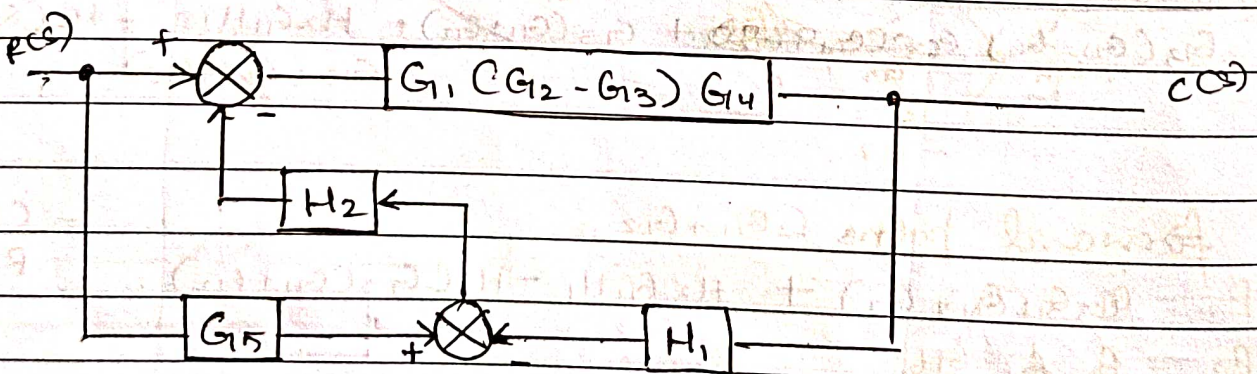
b)



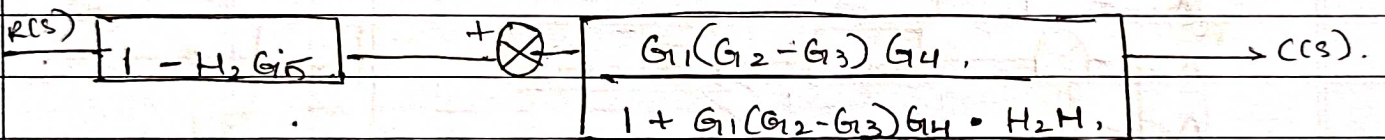
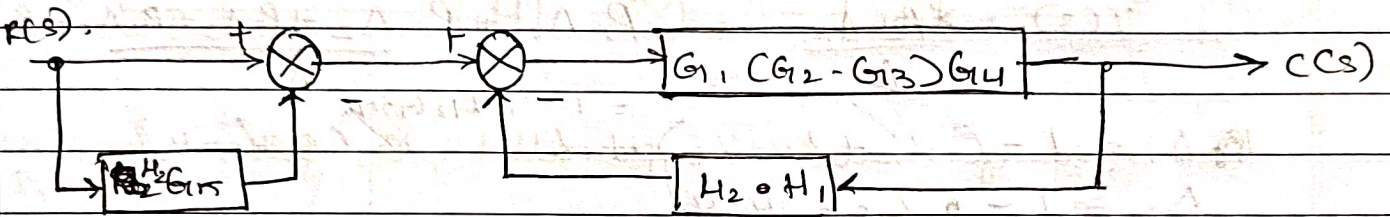
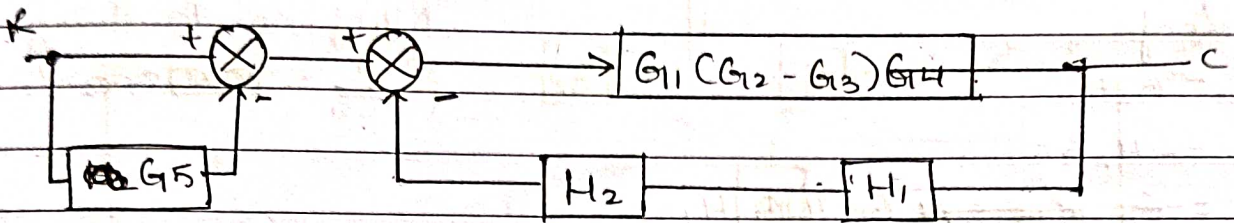
Combining blocks in parallel.  $G_2$  &  $G_3$



Combining blocks  $G_1$ ,  $G_2 - G_3$  &  $G_4$  in Series.



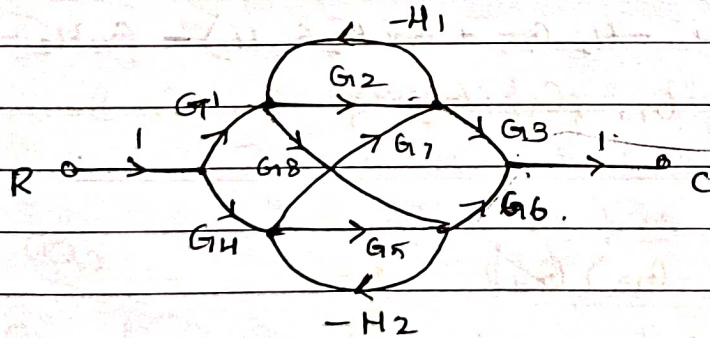
- Splitting summing point.



06

$$\frac{C(s)}{R(s)} = \frac{1 - H_2 G_5 \cdot G_1 (G_2 - G_3) G_4}{1 + G_1 (G_2 - G_3) G_4 \cdot H_2 H_1} //$$

c)



forward paths.

$$P_1 = G_1 G_2 G_3$$

$$P_2 = G_2 G_5 G_6$$

$$P_3 = G_1 G_8 G_6$$

$$P_4 = G_4 G_7 G_3$$

$$P_5 = -G_1 G_2 H_1 G_8 G_6$$

$$P_6 = -G_4 G_5 H_2 G_7 G_3$$

Loops

$$L_1 = -G_2 H_1$$

$$L_2 = -H_2 G_5$$

$$L_3 = -\cancel{G_1 H_1 G_8 H_1} G_8 H_2 G_7 H_1$$

No of non touching loops =

$$L_0 = \cancel{L_1} \cdot \cancel{L_2} \cdot \cancel{L_3}$$

$$T(s) = \frac{\sum P_k \Delta_k}{\Delta} = \frac{P_1 \Delta_1 + P_2 \Delta_2 + P_3 \Delta_3 + P_4 \Delta_4 + P_5 \Delta_5 + P_6 \Delta_6}{\Delta}$$

$$\Delta_1 = 1 - (L_1 + L_2 + L_3) + L_0 = 1 - (G_2 H_1 - H_2 G_5 - G_8 H_2 G_7 H_1)$$

$$\Delta_2 = 1 - 0 \cdot G_8 G_7 H_2 H_6 + L_2/L_3$$

$$\Delta_3 = 1$$

$$\Delta_4 = 1$$

$$\Delta_5 = 1$$

$$\Delta_6 = 1$$

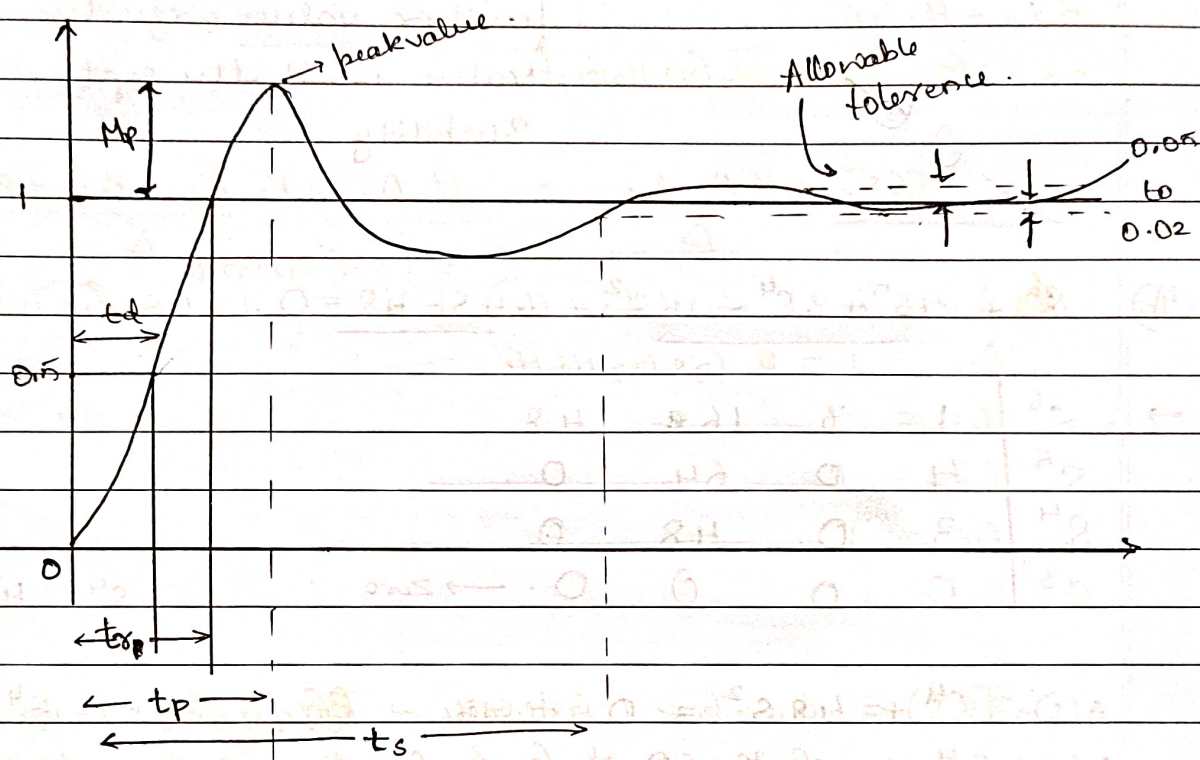
1

$$T(s) = \frac{G_1 G_2 G_3 \cdot 1 - G_8 H_2 G_7 H_6 + G_4 G_5 G_6 \cdot 1 - G_8 G_7 H_2 H_6 + G_1 G_2 G_6 + G_4 G_7 G_3 - G_1 G_2 H_1 G_8 G_6 - G_4 G_5 H_2 H_6}{1 - (G_2 H_1 - H_2 G_5 + G_8 H_2 G_7 H_1) - G_2 H_2 - H_2 G_5}$$

ob

## Part - B.

4a)



- a) **Delay time:** It is a time take for the system to respond or time take for response to attain half of the value of ~~response~~ ~~time~~ or complete value.
- b) **Rise time:** It is time taken for response of time to reach unity. 0-90% for overdamped and 0-100% for underdamped.
- c) **Peak time:** It is time taken for response of time to reach maximum overshoot of highest peak value ~~after waiting~~ from the beginning.

d) Maximum Overshoot: It is the maximum value obtained after reaching unity and all the further values are less than Maximum value until the system attains stability.

$$4b) s^6 + 4s^5 + 3s^4 - 16s^2 - 64s - 48 = 0.$$

$s^6$	1	3	16	48
$s^5$	4	0	64	0
$s^4$	3	0	48	0
$s^3$	0	0	0	0

$\rightarrow$  Zero.

$$s^4 = \frac{4 \times 3 - 1 \times 0}{4}$$

$$A(s) \Rightarrow 3s^4 + 48s^2 = 0 \quad \div 16$$

$$A(s) \Rightarrow s^4 + 16s^2 = 0$$

$$\frac{dA(s)}{ds} = 4s^3 + 32s = 0$$

ds

$s^6$	1	3	16	48
$s^5$	4	0	64	0
$s^4$	3	0	48	0
$s^3$	4	0	32	0
$s^2$	0	24	0	0
$s^1$	0	0	0	0

$s^6$	1	3	16	48
$s^5$	4	0	64	0
$s^4$	3	0	48	0
$s^3$	4	0	32	0
$s^2$	0	24	0	0
$s^1$	24	0	0	0
$s^0$	24	0	0	0

$$A'(s) = 24s = 0$$

$$s = 24$$

∴ As all the values in the System is positive  
and the value of  $s = 24$   
The system is stable.

-04-

$\frac{28}{30}$

J. Hankey  
2/12/22

III<sup>rd</sup> Internals.

## Part-A.

$$1a) \quad G(s) \cdot H(s) = \frac{20}{s(1+0.1s)}$$

Step: Arrange  $G(s) \cdot H(s)$  in time form.

$$G(s) \cdot H(s) = \frac{20}{s(1+0.1s)}$$

Step 2: Identify the factors.

$$1) \quad K = 20 \Rightarrow 20 \log_{10} K = 20 \log_{10} (20) = 26.020 \text{ dB/decade}$$

$$2) \quad \text{No of poles at origin} = 1.$$

$$3) \quad \text{Simple pole; } \frac{1}{s} = -20 \text{ dB/decade } \omega = 0.1$$

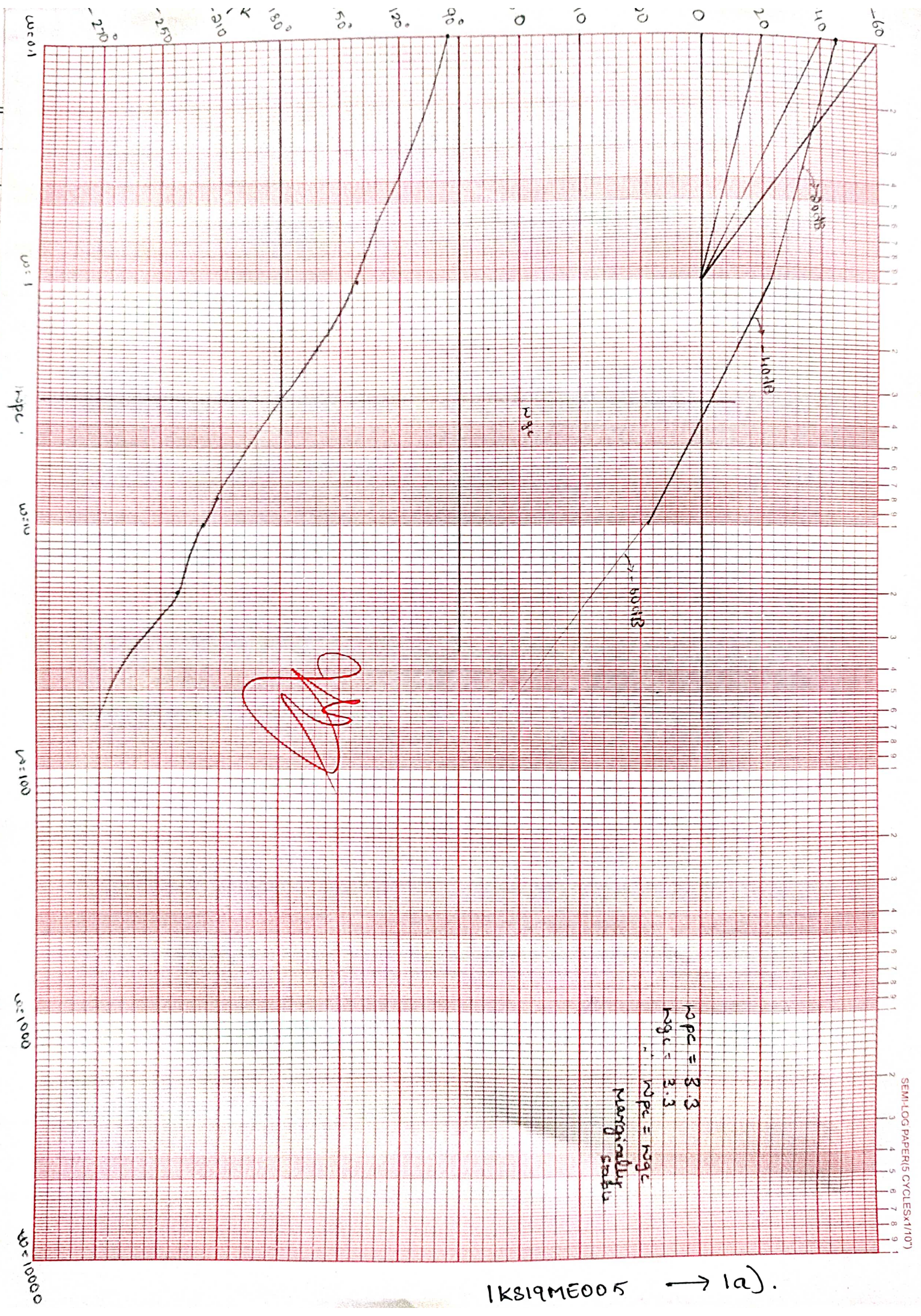
$$2) \quad \text{simple pole, } \frac{1}{1+0.1s} = T_1 = 0.1, \omega_{c2} = 1 = 10 \text{ dB/decade}$$

$$-20 - 20 = -40 \text{ dB/decade}$$

Step 3: Magnitude of poles.

Range of $\omega$ .	$0.1 < \omega < 10$	$1 < \omega < 10$	$10 < \omega < \infty$
Resultant.	-20 dB	-40 dB	-60 dB





IKSIQME005 → 1a).

Step 4: Phase angle.

$\omega$	$1/j\omega$	$-\tan^{-1} \omega$	$-\tan^{-1} 0.1\omega$	$\phi_R$
0.1	$-90^\circ$	$-5.71^\circ$	$-0.572^\circ$	$-96.282$
1	$-90^\circ$	$-45^\circ$	$-5.71^\circ$	$-140.71$
2	$-90^\circ$	$-63.43^\circ$	$-11.30^\circ$	$-164.73$
8	$-90^\circ$	$-82.87^\circ$	$-38.65^\circ$	$-211.52$
10	$-90^\circ$	$-84.28^\circ$	$-45^\circ$	$-219.28$
20	$-90^\circ$	$-87.13^\circ$	$-63.43^\circ$	$-240.56$
$\infty$	$-90^\circ$	$-90^\circ$	$-90^\circ$	$-270^\circ$

06  
 $\omega_{gc} = \underline{\underline{3.3 \text{ rad/sec}}}$

1b)  $G(s) = \frac{80}{s(s+2)(s+20)}$

$GM = ?$

$\omega_{gc} = ?$ ,  $\omega_{pe} = ?$  Comment on stability.

Step 1: Arrange  $G(s) \cdot H(s)$  in time form.

$$G(s) \cdot H(s) = \frac{80}{s(s+2)(s+20)}$$

$$= \frac{80/40}{s(1+0.5s)(1+0.05s)}$$

$$G(s) \cdot H(s) = \frac{2}{s(1+0.5s)(1+0.05s)}$$

Step 2: Identify factor's.

1)  $K = 2$ .  $20 \log K \Rightarrow 20 \log 2 = 6.02 \approx 6 \text{ dB/decade}$

2). No of poles at origin =  $\frac{1}{s} = -20 \text{ dB/decade}$ .

3) Simple poles,  $\frac{1}{1+0.5s} = T_1 = 0.5 \Rightarrow \omega_{c1} = \frac{1}{0.5} = 2 \text{ rad/sec}$

$\Rightarrow -20 - 20 \text{ dB/sec} \Rightarrow -40 \text{ dB/sec}$

4) Simple pole,  $\frac{1}{1+0.05s} \Rightarrow T_2 = 0.05 \Rightarrow \omega_{c2} = \frac{1}{0.05} = 20 \text{ rad/sec}$

$-20 - 20 \text{ dB/sec} = -60 \text{ dB/sec}$

Step 3 = Magnitude of  $\omega$ .

Range of  $\omega$   $0 < \omega < 2$

$2 < \omega < 20$

$20 < \omega < \infty$

Resultant.  $-20$

$-40$

$-60$

Step 4: Phase angles.

$\omega$	$1/j\omega$	$-\tan^{-1} 0.5\omega$	$-\tan^{-1} 0.05\omega$	$\phi_R$
0.1	$-90^\circ$	$-2.86$	$-0.28$	$-93.14$
0.2	$-90^\circ$	$-5.71$	$-0.57$	$-96.28$
1	$-90^\circ$	$-26.56$	$-2.86$	$-119.42$
2	$-90^\circ$	$-45$	$-5.71$	$-140.71$
5	$-90^\circ$	$-68.19$	$-14.03$	$-172.22$
8	$-90^\circ$	$-75.96$	$-21.30$	$-187.76$
10	$-90^\circ$	$-78.69$	$-26.56$	$-195.25$
20	$-90^\circ$	$-84.28$	$-45$	$-219.28$
$\infty$	$-90^\circ$	$-90^\circ$	$-90$	$-270^\circ$



1K519ME005 1c)

Gain Margin = 22dB/decade.

Phase Margin =  $41^\circ$

$\omega_{pc} = 6.8 \text{ rad/sec}$

$\omega_{gc} = 1.9 \text{ rad/sec}$ .

as  $\omega_{gc} > \omega_{pc}$ .

The ~~system~~ system is stable.

1c) 
$$\frac{K}{s(s+2)(s+10)} = G(s).$$

Step: Arrange  $G(s) \cdot H(s)$  in time form.

$$G(s) \cdot H(s) = \frac{K}{s(2)(1+0.5s)(10(1+0.1s))}.$$

$$G(s) \cdot H(s) = \frac{K/20}{s(1+0.5s)(1+0.1s)}.$$

12.53

Step 2: ~~As~~ Identify factors.

1)  $K' = \frac{K}{20} \Rightarrow 20 \log_{10} K' = ?$

2) No of poles at origin =  $\frac{1}{s} \Rightarrow -20 \text{ dB/decade at } \omega = 0.1$ .

3) Simple poles =  $\frac{1}{1+0.5s} = T_1 = 0.5 \Rightarrow \omega_{c1} = \frac{1}{T_1} = \omega_{c1} = \frac{1}{0.5}$   
 $\omega_{c1} = 2 \text{ rad/sec}$ .

$\Rightarrow \omega \Rightarrow -20 \text{ dB} - 20 \text{ dB} = -40 \text{ dB}$ .

4) Simple poles =  $\frac{1}{1+0.1s} = T_2 = 0.1 \Rightarrow \omega_{c2} = \frac{1}{T_2} \Rightarrow \frac{1}{0.1} = 10 \text{ rad/sec}$

$\Rightarrow -40 \text{ dB} - 20 \text{ dB} = -60 \text{ dB}$ .

Step 3: Magnitude of  $\omega$ .

Range of $\omega$	$0 < \omega < 2$	$2 < \omega < 10$	$10 < \omega < \infty$
Resultant	-20	-40	-60

Step 4: Phase angles

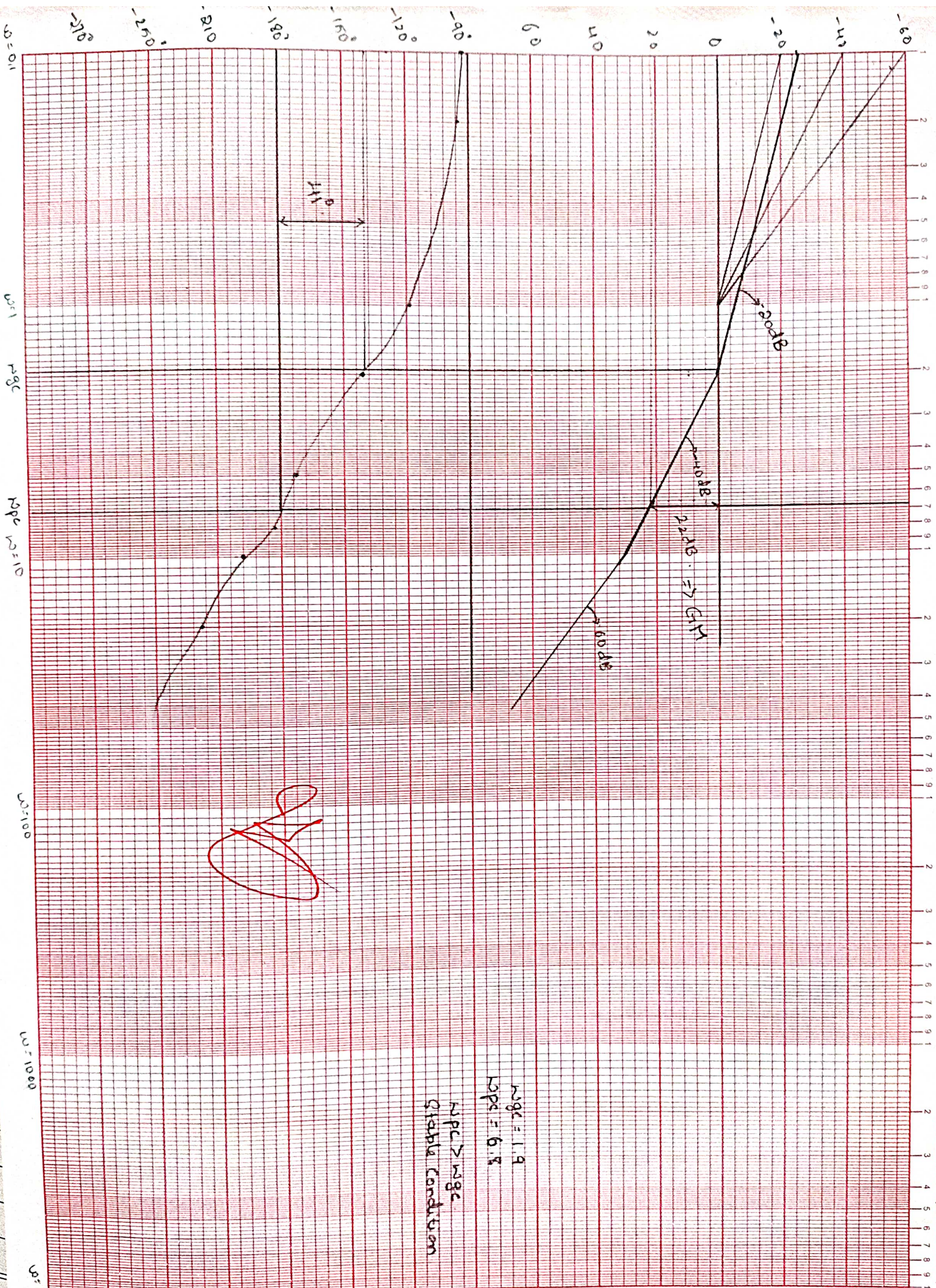
$\omega$	$1/j\omega$	$-\tan^{-1} 0.5\omega$	$-\tan^{-1} 0.1\omega$	$\phi_R$
0.1	$-90^\circ$	-2.86	$-0.572$	-93.43
0.2	$-90^\circ$	-5.71	<del>-1.145</del>	-96.85
1	$-90^\circ$	-26.56	<del>-5.71</del>	-122.27
2	$-90^\circ$	-45	<del>-11.30</del>	-146.3
5	$-90^\circ$	-68.19	<del>-26.56</del>	-184.75
8	$-90^\circ$	-75.96	-38.65	-204.11
10	$-90^\circ$	-78.69	-45	-213.69
20	$-90^\circ$	-84.28	-68.43	-237.71
$\infty$	$-90^\circ$	$-90^\circ$	$-90^\circ$	$-270^\circ$

$$20 \log k' = \text{---} 22$$

$$k' = \text{---} 12.58$$

$$\frac{k}{20} = \text{---} 12.58 \quad k = 251.6$$

06



$MPC > MGC$   
 Stable condition

11KSIAME005 16)

Part - B

$$4a) G(s) \cdot H(s) = \frac{K}{s(s+2)(s+4)(s+6)}$$

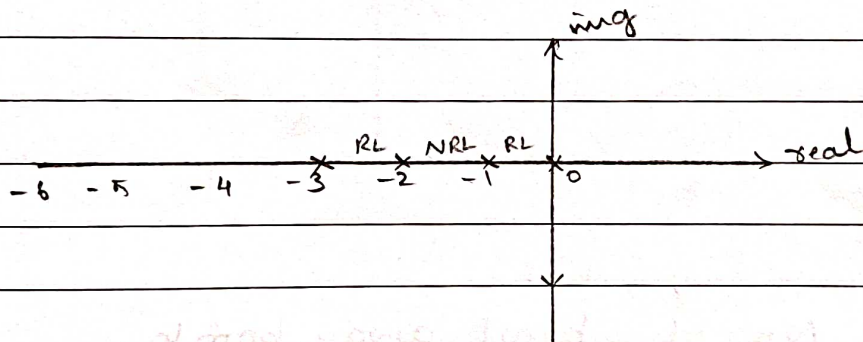
→ No of poles = 4

No of zero's = 0.

Starting point of poles = 0, -1, -2, -3.

terminating points of poles =  $\infty, \infty, \infty, \infty$ .

Step 2:



Step 3: Angles of Asymptotes.

$$\theta = \frac{(2q_i + 1) \times 180}{P - Z}$$

$$q_1 = 0 \quad \theta_1 = \frac{(2(0) + 1) \times 180}{4 - 0} = 45^\circ$$

$$q_2 = 1 \quad \theta_2 = \frac{(2(1) + 1) \times 180}{4} = 135^\circ$$

$$q_3 = 2 \quad \theta_3 = \frac{(2(2) + 1) \times 180}{4} = 225^\circ$$

$$q_4 = 3 \quad \theta_4 = \frac{(2(3) + 1) \times 180}{4} = 315^\circ$$

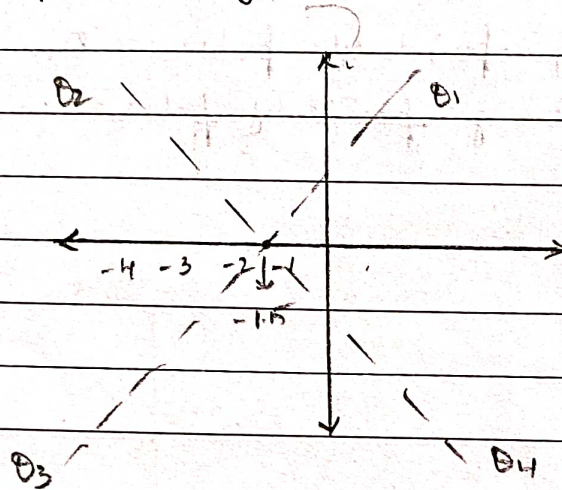


Step 4: Position of Centroid.

$$\text{centroid} = \frac{\text{Sum of poles} - \text{Sum of Zero}}{P - Z}$$

$$\Rightarrow \frac{0 - 1 - 2 - 3 - 0}{4} = \frac{-6}{4} = -1.5$$

$\therefore$  The position of Centroid = -1.5.



Step 5: No of break away points.

$$1 + G(s) \cdot H(s) = 0$$

$$1 + \frac{K}{s(s+2)(s+4)(s+6)} = 0$$

$$s(s+2)(s+4)(s+6) + K = 0$$

$$(s^2 + 2s)(s+4)(s+6) + K = 0$$

$$(s^3 + 2s^2 + 8s + 4s^2)(s+6) + K = 0$$

$$s^4 + 6s^3 + 2s^3 + 12s^2 + 8s^2 + 48s + 4s^3 + 24s^2 + K = 0$$

$$s^4 + 10s^3 + 44s^2 + 48s + K = 0$$

$$\frac{dK}{ds} = 4s^3 + 36s^2 + 88s + 48 + K = 0 \quad \div 4$$

$$\frac{dK}{ds} = s^3 + 9s^2 + 22s + 12 + K = 0$$

$$K = -s^3 - 9s^2 - 22s + 12 = 0.$$

~~$x_1 = 0$~~   $s_1 = 0.45$

$K = 0.18.$

$s_2 = -4.72$

$K = 421.49.$

$s_3 = -4.72$

~~0.5~~

$\frac{23}{30}$

~~Thamara~~  
26/12/21